

## 5. PROBLEM № 11: WATER DROPLETS

SOLUTION OF NEW ZEALAND

### Problem № 11: Water Droplets

/Power Point Presentation/

#### The problem

➤ *If a stream of water droplets is directed at a small angle to the surface of water in a container, droplets may bounce off the surface and roll across it before merging with the body of water. In some cases the droplets rest on the surface for a significant length of time. They can even sink before merging. Investigate these phenomena.*

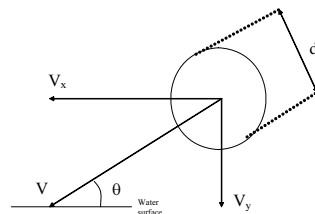
#### Definition of question

- **Droplets**; spherical balls of water
- **Bounce**; the droplets, after impact with the water surface must rebound off.
- **Roll**; the droplets don't coalesce with the water surface as they float on the surface while rotating.
- **Merging**; when the droplet coalesces with the water in the container.
- **Investigate**; Explore the nature as to why these phenomena happen and what will affect these phenomena.

#### Parameters of the problem

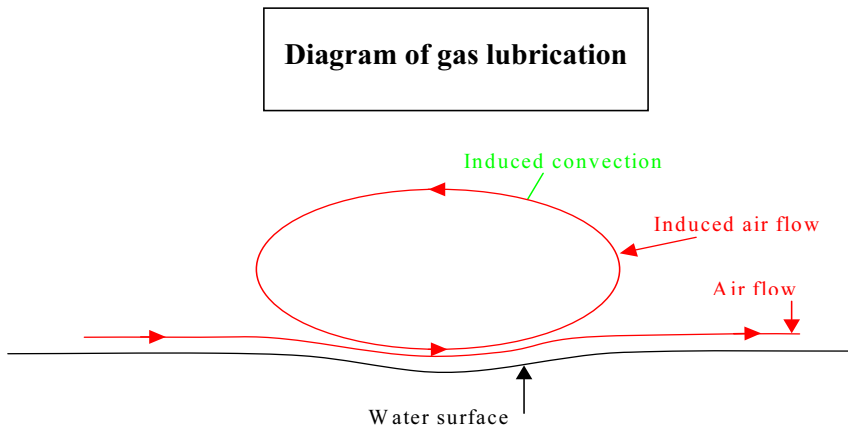
##### Diagram of a droplet

- Droplet diameter ( $d$ )
- Impact velocity ( $V$ )
- Vertical component of  $V$  ( $V_y$ )
- Horizontal component of  $V$  ( $V_x$ )
- Bounce height ( $b$ )
- Incident angle ( $\theta$ )



## Theory (why the droplet doesn't mix with the water surface)

- The droplet doesn't coalesce with the water surface.
- The reason for this non-coalescence is because of gas lubrication.
- This is when a very thin layer of air is trapped between the interface.



## Theory (bouncing)

- The effect of gas lubrication has to be sufficient to maintain separation.
- The downwards momentum makes droplet spread out, creating a dimple in the water surface.
- They recoil to their original states, if this is forceful enough, the droplet will rebound of the water surface.

## Sequence of droplet bounce



## Theory (rolling)

- If  $V_x$  is large enough to maintain sufficient gas lubrication, the droplet won't coalesce.
- But if  $V_y$  is too small the droplet doesn't exert a large enough force on the water surface.
- So it will instead roll across the surface until  $V_x$  becomes too small.
- Then it will coalesce.

## Theory of sinking droplets

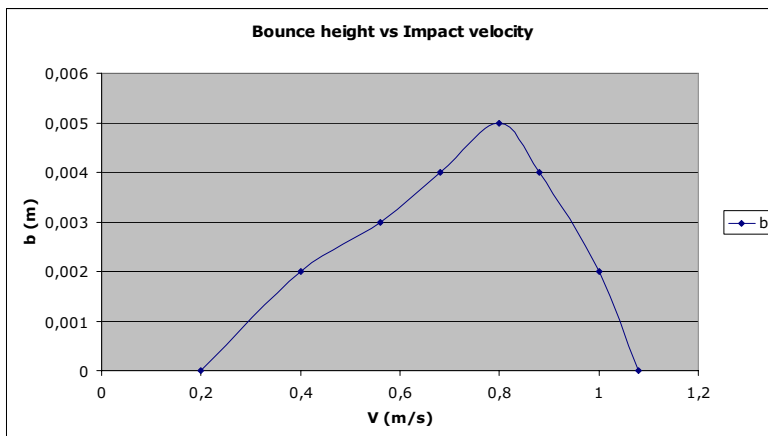
- Heat capacity of a droplet is very small.
- This causes the density to drop.
- It also increases the surface tension of the droplet.
- The droplet must break the surface.
- This can be done by weight ( $>4\text{mm}$  d) or downwards momentum.

## Theory of sinking droplets

- For this to occur the droplet cannot be allowed to coalesce.
- This non-coalescence occurs again because of gas lubrication.
- Initial air flow under the droplet causes the droplet to rotate.
- A layer of air will fully enclose the droplet and circulate around it maintaining separation.

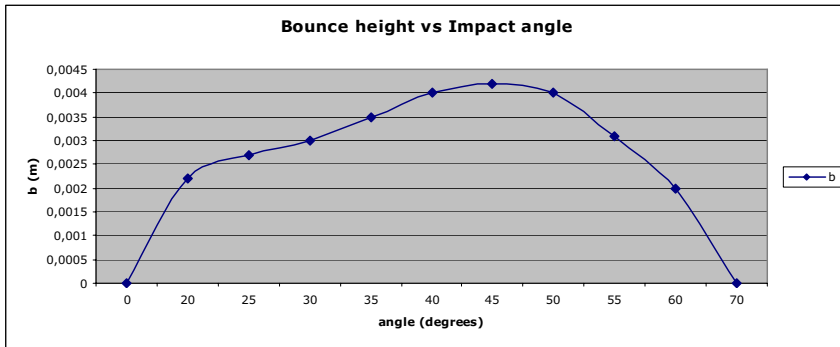
## Theory (V)

- The more kinetic energy it has the more kinetic energy can be converted into potential energy.
- Therefore the higher it can bounce.
- The greater V the longer the collision time.
- The more energy loss.
- The lower the bounce height.
- There will be optimum V for any given  $\theta$ .



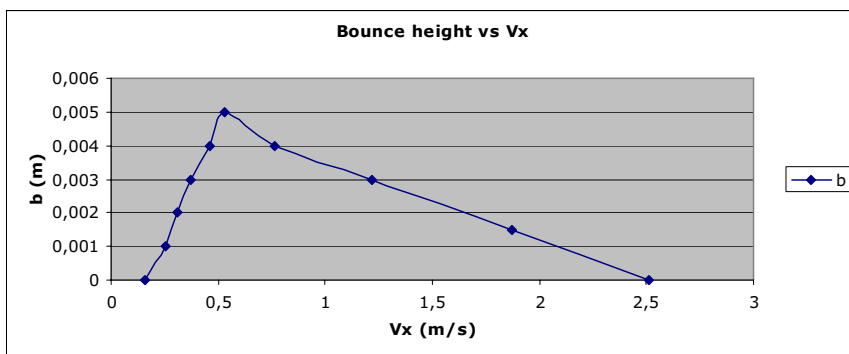
## Theory ( $\theta$ )

- The less  $\theta$  is the greater  $V_x$  is in relation to  $V_y$ .
- The greater  $\theta$  is the more force the droplet can apply to the surface
- So there is also an optimum  $\theta$  for a given  $V$ .
- At a lower  $V$  a greater  $\theta$  is better and at a higher  $V$  a smaller  $\theta$  is better.



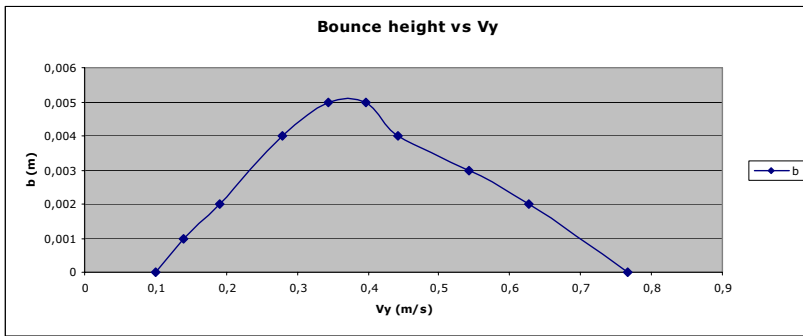
## Theory ( $V_x$ )

- Greater  $V_x$  means better gas lubrication.
- Hence more downwards force it can overcome.
- Hence the higher it can bounce.
- Greater  $V_x$  also means greater  $V$  hence a longer the collision time.
- Therefore the more energy loss there is.



## Theory ( $V_y$ )

- Greater  $V_y$  means more downwards force exerted by the droplet.
- The effect of gas lubrication has to also increase to cope with the extra downwards force.
- Greater  $V$  also means a longer collision time.



## Theory (d)

- Smaller  $d$  means a higher ratio of surface tension to volume.
- Therefore the more robust the droplet is.
- Therefore the higher  $V$  the droplet can withstand and not break up.
- Also the more efficient the collisions are.

## Video of small/large droplets

## Conclusion

- The smaller the droplet diameter the higher it bounces
- There will be an optimum impact velocity ( $V$ ) for any given angle ( $\theta$ ).
- To gain the highest bounce an increase in  $V_y$  must have an increase in  $V_x$ .
- For the longest roll time a large  $V_x$  is needed with a small  $V_y$  and if possible a forwards spin.
- For sinking the faster the spin and the larger the droplet (assuming it stays spherical) the better.

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