



PROBLEM 25: DAMPED PENDULUM

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PROBLEM

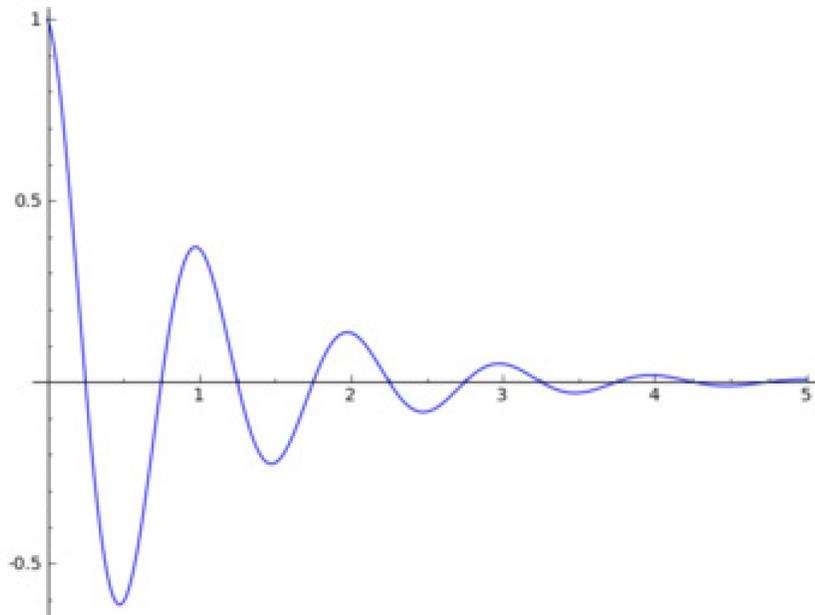
Damped pendulum

- Determine the **decay time** of a **pendulum**



DEFINITIONS

- Decay time – amount of time it takes for the pendulum to be at rest at the equilibrium point
- Pendulum – a mass attached to a string and allowed to swing in simple harmonic motion



SIMPLE HARMONIC MOTION

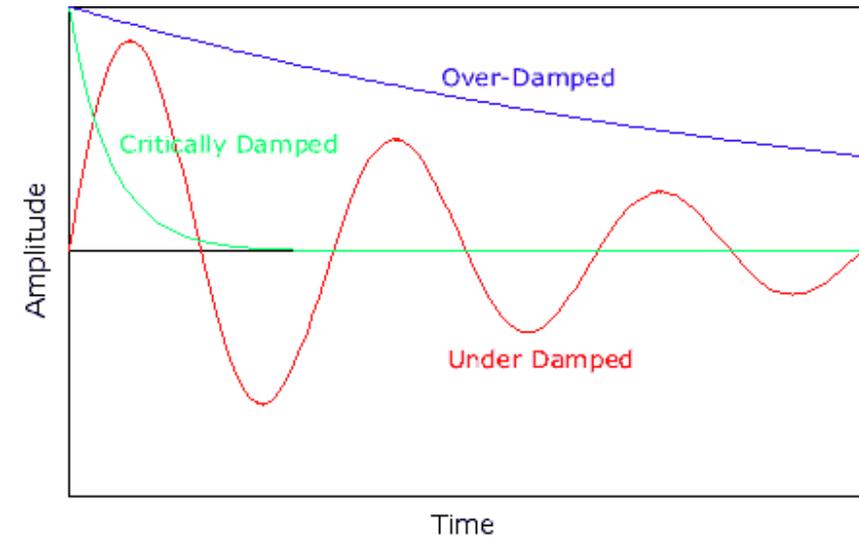
- Special type of motion
 - Restoring force is proportional to the displacement
 - Restoring force acts in the direction opposite of the displacement
- There is periodic motion or oscillation motion
- This means the object always repeatedly returns to a point in its motion
- In simple harmonic motion dampening forces are not considered

COMPLEX HARMONIC MOTION

- Does consider dampening forces
- Dampening forces slow the object down
- Far more real world applications than simple harmonic motion as some form of dampening forces almost always act on an object

DAMPENING FORCES

- Three different types of dampening forces:
 - Critically dampened – The system returns to equilibrium as quickly as possible
 - Overdampened – The system returns (exponentially decays) to equilibrium
 - Underdampened – The system oscillates with the amplitude decreasing too zero
- Real life application
 - Bungee
 - Swings



PENDULUM

- A mass attached to a string and allowed to swing in simple harmonic motion
- A pendulum is in complex harmonic motion
 - Returning to equilibrium point
 - There are dampening forces acting on the pendulum

$$T = 2\pi \sqrt{\frac{L}{g}}$$

T = Time period
L = Length
g = acceleration due to gravity

HYPOTHESIS

- The higher the friction the less time it will take to reach a point of rest at its equilibrium point
 - Friction will be increased if the object has larger surface area and thus there is more air resistance
 - The mass of the object will increase the tension in the string and thus the friction of the string

VARIABLES

- Standardized
 - String length (40.4 cm)
 - Acceleration to due gravity (9.81 m/s²)
 - Initial angle
- Independent:
 - Mass
 - Surface area
- Dependent:
 - Decay time

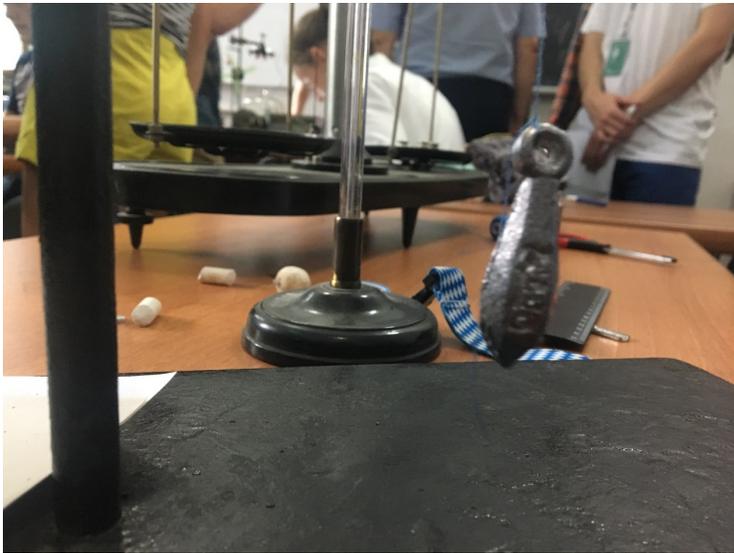
$$T = 2\pi \sqrt{\frac{L}{g}}$$



PENDULUM OBJECTS

Used three different objects as a pendulum

Metal Bob



Metal Ball



Apple



EXPERIMENTAL SET UP



String

Object attached
to pendulum

Camera



EXPERIMENT

Time-lapse of experiment



The distance the pendulum moves gets slightly shorter every period

Does not change:
Period
String length
Gravity



RESULTS

- Metal ball: 17 minutes
 - Metal ball had the lowest mass and the lowest air resistance
- Metal bob: 11 minutes
 - Metal bob had second highest mass and second highest air resistance
- Apple: 10 minutes
 - Apple had highest air resistance and highest mass



CONCLUSION

- Ranking of decay:
 - Apple
 - Metal Bob
 - Metal Ball
- Matched the hypothesis, air resistance and mass both had an effect





THANK YOU FOR LISTENING

